

Metamaterials in musical acoustics: A modified frame drum

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Metamaterials in musical acoustics: A modified frame drum

Rolf Bader,^{a)} Jost Fischer, Malte Münster, and Patrick Kontopidis

Institute of Systematic Musicology, University of Hamburg, Neue Rabenstrasse 13, 20354 Hamburg, Germany

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Mechanical musical instruments have a restricted timbre variability compared to electronic instruments. Overcoming this is the aim of extended playing techniques as well as building more sophisticated musical instruments in recent years. Metamaterials might be a way to extend timbre of mechanical instruments way beyond their present sound capabilities. To investigate such possibilities, a frame drum is manipulated to achieve different sounds. On the drum membrane of 40 cm diameter, a ring of masses is attached in three diameters, 8, 10, and 12 cm with 10 masses each, leading to a cloaking behaviour of vibrations from within the ring into the area outside the ring and vice versa, as shown by microphone-array and high-speed laser interferometry measurements. The resulting sounds have a band gap between about 300 and 400 Hz to about 700–800 Hz, depending on the ring diameter. The 8 cm diameter ring shows the strongest amplitude attenuation in the band gap. Still, when striking the membrane outside the ring, it sounds like a regular drum. This leads to a tremendously increased variability of musical articulations, especially when striking in the ring, as a band gap sound cannot be produced by a regular drum. © 2019 Acoustical Society of America. <https://doi.org/10.1121/1.5102168>

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I. INTRODUCTION

Metamaterials have not explicitly been used in musical instruments to this point. Still, the complex geometry of musical instruments might lead to reconsidering them. Although the fan bracing of guitars or the bracing of piano soundboards is built mainly for the purpose of stability, such regular substructures might lead to a behaviour meeting conditions of the concept of metamaterials. Indeed, pitch glides of Chinese gongs,¹ the brassiness of crash cymbals² or tam-tams,³ or the increased brightness of Balinese *gamelan gender* bronze plate⁴ are caused by complex geometries.

Metamaterials in musical instruments can be used to change the instrument sound considerably. Changing existing instrument geometries can lead to added band gaps in their spectrum, and using several such band gaps will lead to a designed sound. With percussion instruments, musical articulation is realized by striking or knocking at different positions on, e.g., drums or cymbals. By adding metamaterial structures to them, the variability of such sounds can be increased considerably.

Membranes used in rock or jazz drum kits, as well as with *tablas* of Indian music or the *pat wain* or the Myanmar *hsain wain* orchestra, often show additional masses attached to them. They are used for different purpose. Jazz drummers use tape and other material to damp especially the snare drum. Also, tom-toms are taped to reduce the loudness as well as the length of their tone. Detuning of these drums plays a minor role since these drums are tuned by tuning pegs at the drum head rim. *Tabla*^{5,6} and *pat wain*⁷ drums are tuned by adding a plate or a special tuning paste, respectively. The aim is twofold; the drum is tuned with respect to its pitch and moreover the overtone spectrum of the drums is

changed to arrive at a more harmonic overtone spectrum of the fundamentally inharmonic spectrum of these percussion instruments. The advantage of a more harmonic spectrum is to increase pitch perception of the drums to use them in melody performance.

Metamaterials have been used with membranes to achieve damping over a large bandwidth,^{8,9} for a review see Ref. 10. With massive rings attached concentric on the membrane, one or only a few resonance frequencies exist up to 1 kHz, which leads to strong damping of the membrane within this range with large peaks at the resonance frequencies. Such applications differ from the concept proposed in this paper in its aims. There a strong overall damping is aimed for, where with musical applications only a partial damping is needed to maintain an audible sound. Also, with such heavy masses, the membrane between the mass and the membrane boundary, as well as the membrane between two rings, can mainly be considered as a spring. As with concentric rings, the distances between the rings, outer boundary and the membrane boundary is a constant for all angles; only one spring length and strength is present. So, these applications differ in principle from the construction and the aims of the dot masses attached asymmetrically on a membrane present in this study.

Circular or more complex shaped geometries might result in a cloaking behaviour, where a traveling incoming wave looks the same in both cases, with the structure and without the structure in its way. Therefore, for an observer behind the structures this structure is invisible.¹¹ Such geometries can also act as cages, where waves in them cannot travel out and vice versa. This has been found in optics¹² and has been applied in acoustics as in Refs. 13 and 14, among others. This behaviour is frequency dependent and a way to build a musical metamaterial, enhancing the articulatory ability of a musical instrument.

In this paper an example of applying metamaterial behaviour to musical instruments is demonstrated using a frame drum. Its results bring on highly interesting new sounds and

^{a)}Electronic mail: r_bader@t-online.de

increased articulatory ability for players. After introducing the constructed instruments, the paper discusses the measurement techniques applied, microphone array and laser interferometry. Increased articulatory possibilities of the new instrument are discussed together with further design possibilities.

II. METHODS

A. Frame drum

A frame drum with a BoPET (biaxially-oriented polyethylene terephthalate) also called mylar drum membrane and a diameter of 40 cm was used. At the drumhead a ring-shaped area (m) with a diameter of 10 cm is separated using a set of 2×10 neodymium magnets sticking at the front and the back of the membrane. The magnets are circular with a diameter of 5 mm and a height of 5 mm (see Fig. 2).

The magnets were chosen because they add a heavy mass to the membrane at distinctive points. When two magnets are attached to each other from the top and bottom side of the membrane the vibrations on the membrane are never strong enough to make the magnets move or fall off, no matter how hard the drum is struck. Additionally, magnets do not damage the membrane during attachment or when removing. They are also quite heavy with respect to their size. Yet a fourth advantage is that they can easily be moved by hand forming new structures. So, musicians would be able to handle them easily. Still, there is a lower distance limit between the magnets, as they will align magnetically. After experimenting with different adhesive fastening techniques, magnets were found to outperform other methods.

The area separated by the magnets is assumed to act as cloaking, separating vibrations inside and outside this area. Therefore, it is expected that waves originating outside the ring will not enter and vice versa. In this case the frequencies and modes of one of the membrane areas are cloaked and do not contribute to the radiated sound. We therefore expect a band gap to appear in some cases where certain frequency regions are not present. The cloaking of a frequency band, the band gap is then caused by a cloaking of regions on the membrane.

B. Laser interferometry

The experimental laser setup is depicted in Fig. 1. A Verdi Single FAP (fiber array package) diode-pumped solid state frequency doubled neodymium vanadate (Nd:YPO_4) laser (LSR) source radiates a beam of wavelength 532 nm and beam diameter of $d_{\text{LSR}} = 2.25 \pm 10\%$ mm. The beam is splitted by a beam splitter (Bs). The splitted beams are directed to planar mirrors (M1) and (M2). Subsequently the beams are expanded via an optical lens system, consisting of a semi-concave lens with focal distance of $f_{\text{L1,L3}} = -16$ mm and a diameter of $d_{\text{L1,L3}} = 10$ mm and a semi-convex lens with focal distance of $f_{\text{L2,L4}} = 300$ mm and a diameter $d_{\text{L2,L4}} = 100$ mm.

The drumhead was manually excited by an impulse hammer. The excitation has been applied outside as well as inside the separated area of the drumhead. The split and widened beams are directed to the drumhead (M) of a frame drum (D). The impulse response leads to a characteristic interference pattern at the drumhead. The pattern is recorded using a high-

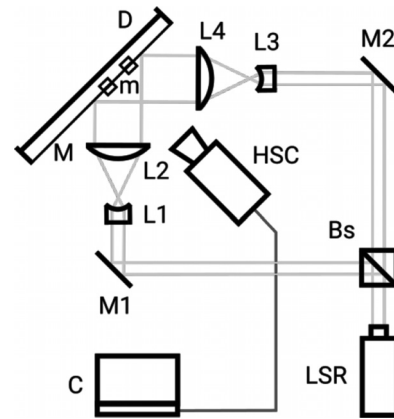


FIG. 1. The experimental setup. (LSR) laser, (Bs) Beam splitter, (M1, M2) planar mirrors, (L1, L3) semi-concave lenses ($f_{\text{L1,L3}} = -16$ mm, $d_{\text{L1,L3}} = 10$ mm), (L2, L4) semi-convex lenses ($f_{\text{L2,L4}} = 300$ mm, $d_{\text{L1,L3}} = 100$ mm), (M) drumhead of the frame drum (D), (m) ring-shaped part of the drumhead, separated utilizing a set of 2×10 Neodymium magnets. (HSC) high-speed camera, (C) analysis using a PC. The beam paths are marked by green lines.

speed camera (HSC) with a frame rate resolution of 10 000 fps. The received data are analyzed utilizing MATHEMATICA on a PC by subtracting adjacent recorded frames.¹⁵

Additionally, the drum head was excited by an actuator, a Brüel & Kjaer Vibration Exciter 4809, again in the middle of the ring and outside with a low frequency of 65 Hz and a high frequency of 918 Hz, two eigenfrequencies of the drum head with magnets on.

C. Microphone array

The sound pressure field of the frame drum was recorded with a microphone array in the near-field, 3 cm in front of the membrane (see Fig. 2). The grid constants of the array are 5 cm in x-direction and 4 cm in y-direction. The microphone array records sound fields with up to 128 microphones with a sampling frequency of 48 kHz and a sample depth of 24 bit simultaneously.

The recorded sound fields are back-propagated to the surface of the membrane using the minimum energy method,¹⁶ a multipole-method assuming as many radiation sources as microphones. It has successfully been used to measure the vibrations of musical instruments^{17,18} (for a review on microphone arrays and back-propagation methods, see Ref. 19).

For the recordings with the microphone array the drum was struck at three positions only, recorded with a single microphone placed 50 cm in front of the membrane opposite, pointing to the drum center in an anechoic environment. Each recording resulted in 120 sound files at the microphone positions. From these the frequency spectra were calculated and all peaks up to 1 kHz were determined. For each of these frequencies the recorded sound field was back-propagated to the surface of the drum.

III. RESULTS

A. Drum modes and traveling waves

The drum was struck at three different positions as it is expected that the ring acts as a cloaking effect to the sound



FIG. 2. (Color online) Modified frame drum positioned in front of the microphone array.

and therefore striking within the ring should keep most of the vibrations within this ring, while striking outside the ring would lead to a strongly reduced energy in the ring. In Figs. 3 and 4 the results of the microphone array recordings and back-propagations are shown considering this point.

The results in Fig. 3 are calculated by first detecting the maximum absolute amplitude of each mode. The local positions of these maxima are accumulated on the membrane for all strikes. Then all points on the membrane showing more than 20% of accumulated maximum points are displayed.

At the top of Fig. 3, the case of striking in the ring is shown. Clearly most maximum points are within the ring. When striking at the ring rim, shown in the middle graph, the distribution of maximum amplitudes is more widespread over the membrane. Finally, with the case of striking outside the ring, shown as the bottom plot in the figure, no considerable maxima are within the ring.

To differentiate this finding with respect to frequency, the amount of absolute amplitude within the ring is shown in Fig. 4 as a fraction of the whole absolute amplitude on the drum. The three curves show the three cases of striking in the ring, at the ring rim and outside the ring. Again, striking in the ring leads to a strong increase of amplitudes within the ring, compared to the cases of striking at the ring rim and outside the ring. Still, this increase only appears above about 400 Hz. As the fundamental frequency of the drum is 34 Hz we can conclude that the low frequencies are not much effected by the ring, while the higher ones clearly are.

Still, the relative high fraction of amplitudes in the ring at very low frequencies are again remarkable. The lowest peak detected at 7 Hz is not audible and most likely refers to the motion of the drum as a whole, so including the wooden frame. This motion is unavoidable as frame drums only

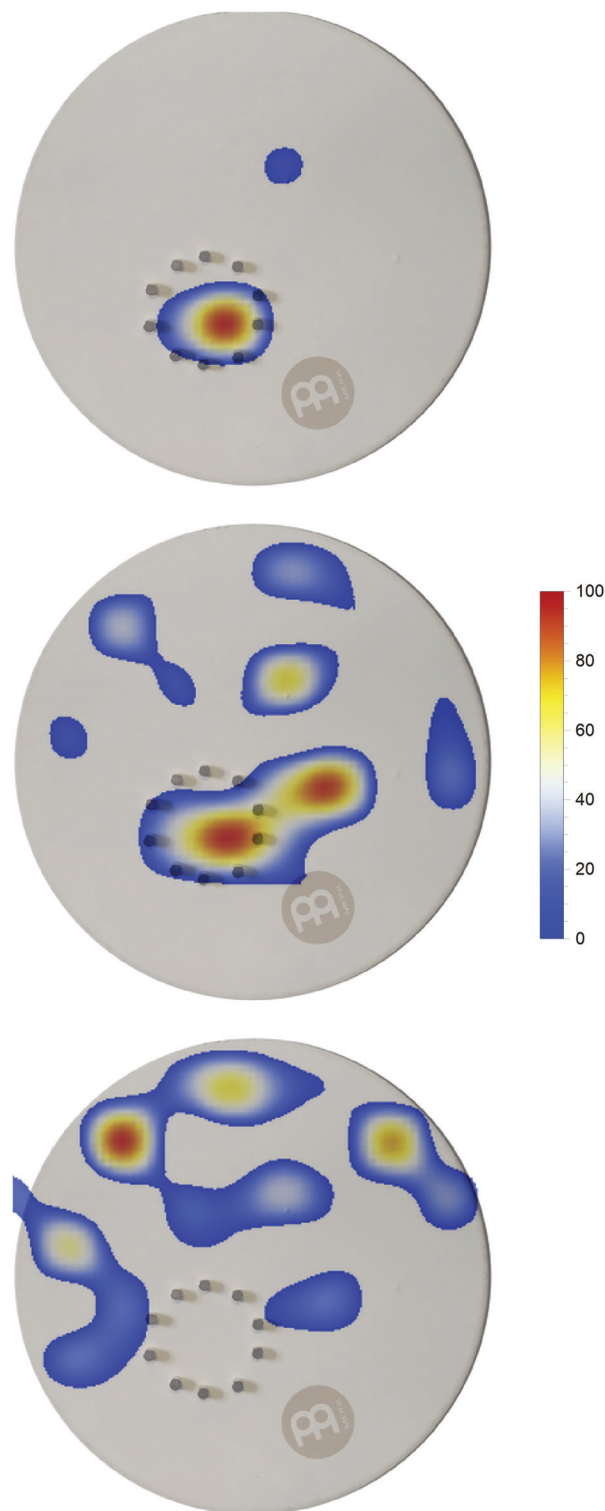


FIG. 3. Density distribution of maximum pressure amplitude values of modes on the drum up to 1 kHz for three hammer strike positions, color bar in percentage of maximum density. Top: strike in the ring, middle: strike at ring rim, bottom: strike outside the ring at the opposite side of the ring. While most maximum values for the strike in the ring are in the ring, very few are within the ring when the drum is struck outside the ring. A medium case is found when striking at the ring rim.

sound when the wooden frame is free. Fixing it strongly, which would avoid this low vibration would lead to a very much damped sound and can therefore not be implemented in an experimental setup.

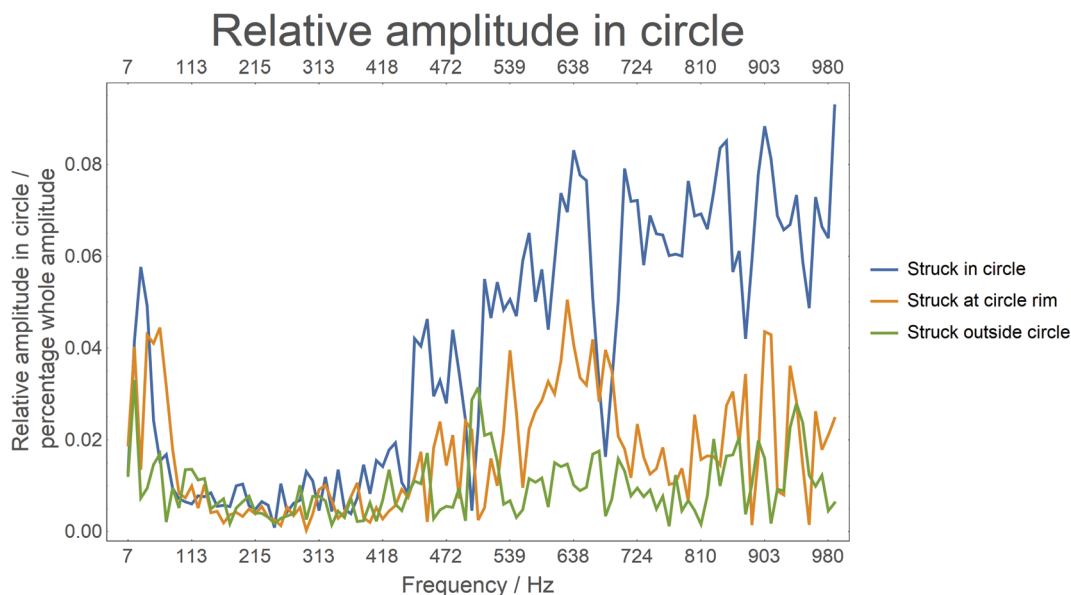


FIG. 4. Frequency-dependent absolute pressure amplitude within the ring compared to total absolute pressure amplitude on the whole drum for three strike cases (a) in the ring (blue), (b) at the ring rim (orange), and (c) outside the ring (green). While for frequencies below around 400 Hz the amplitude strength of the three cases are about the same, above about 400 Hz the amplitude strength within the ring strongly depends on the strike position. Strikes in the ring have stronger amplitudes there than strike at the rim with strike outside the ring showing least amplitudes in the ring.

Still, the very low frequencies at 34 Hz, the “monopole” vibration and around 65 Hz, the “dipole” vibration again show much more relative amplitude within the ring in the cases of striking in the ring and striking at its rim, compared to the case of striking outside the ring.

The reason for this behaviour can be found when examining the modes more closely. The very low modes need to make the ring region move, too, as the anti-node regions are large, with 34 Hz it basically covers the whole membrane, with the 65 Hz “dipole” case the membrane is split into two regions about half the membrane each. Of course, due to the ring no monopole and dipole modes exist as in the case of a isotropic membrane.

The higher modes above the dipole, quadrupole, octupole, and many other more complex modes with an integer number of axial and circular nodal lines, these modes can deform in such a way to avoid the motion of the ring region nearly completely. This holds for all three strike cases. It seems that even when striking in the ring, the ring is not able to maintain a vibration of these frequencies. The small leakage of vibrations leaving the ring is then taken over by the rest of the membrane leading to very similar motion compared to the case when striking outside the membrane.

To confirm these findings in Fig. 5 laser interferometry measurements for the case of striking in the ring are shown. The strike’s transient is displayed as six snapshots at 0, 0.2, 0.6, 1, 3, and 6 ms. Each black/white line indicate an amplitude increase of one wavelength of the used laser light. Therefore, many rings do not indicate an amplitude ripple but a steep slope of the amplitude.

Starting at 0 ms, the strike leads to a circular wavefront leaving the strike point, shown at 0.2 ms. At about 0.6 ms this circular wavefront meets the ring rim. Here, it is scattered and at the open rim positions new wavefronts start, as expected. At 1 ms these wavefronts form another wavefront

outside the ring, slightly ripped as this wavefront is formed from a finite number of elementary waves according to the Huygens principle. Two cases at 1 and 3 ms show the wavefront outside the ring becoming more and more complex as the wavefront is then already reflected at the drum boundaries and leads to a complex waveform.

It can be seen at 1 ms that the ring still has a strong amplitude, much stronger than that leaving the ring. This picture continues at 3 and 6 ms supporting the findings from above. Again, most vibrations are overall kept out of the ring when striking.

The same transient time development when striking outside the ring is shown in Fig. 6. Again at 0 ms a circular wave leaves the impact point which arrives at the ring at about 0.6 ms. At 1 ms it can be seen that the strong amplitude is still present outside the ring while only a small fraction enters the ring. This continues at 3 ms. At 6 ms there is some energy left in the ring likewise, which is expected from the above findings, namely that for very low frequencies at 34 and 65 Hz, the ring region is also moving with some amplitude. Overall, most vibrations keep out of the ring when striking.

To differentiate the low/high frequency difference further, the drum is driven by a shaker in and outside the ring at two frequencies, 65 and 918 Hz. In Fig. 7 snapshots of the vibrations are shown at maximum amplitudes of the sinusoidal vibrations. On the top row the 65 Hz cases are shown, on the left the case when driving in the ring, on the right when driving at outside the ring. Clearly in both cases broad vibrations can be seen, indicating a distorted dipole motion. Although when driving inside the ring the amplitude is stronger inside than outside, some amplitude is still outside. When driving outside, the amplitude is about equally distributed. This is in accordance with the findings of the microphone array, especially with that of Fig. 4. There in all

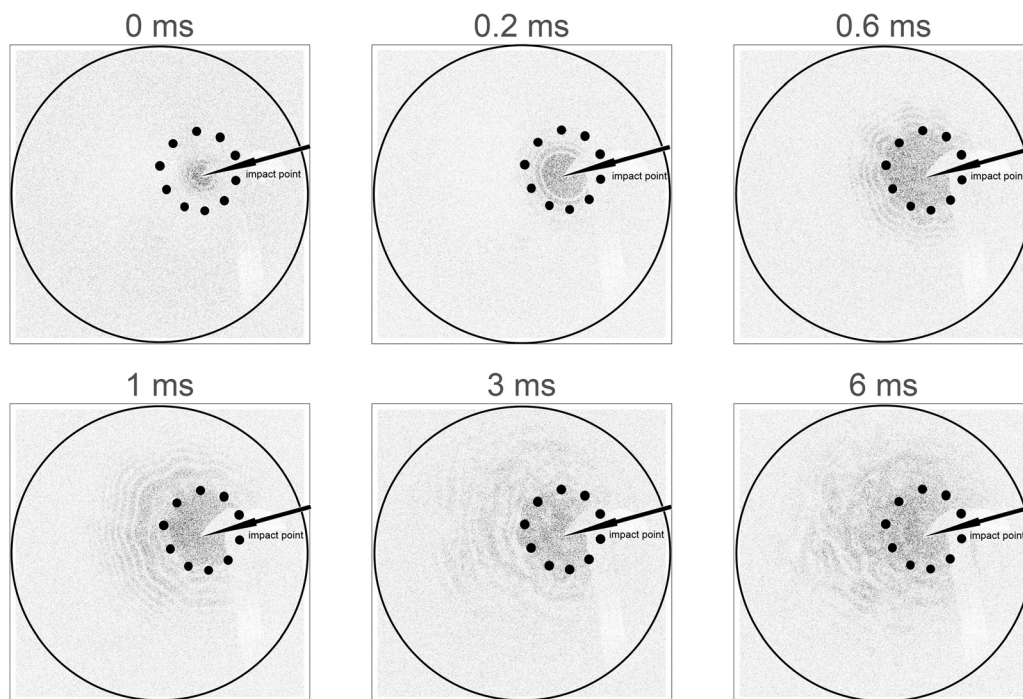


FIG. 5. Laser interferometry time-dependent measurement of the initial transient of a hammer strike on a drum with a separated circular area for several time steps. One transition between black and white corresponds to a displacement amplitude of half the laser light wavelength. At 0 ms a circular wave leaves the strike point which meets the ring boundary at about 0.2 ms. The boundary elements lead to a split of the ring and the appearance of Huygens wave fronts outside the ring beyond 0.6 ms. At 3 ms the reflected waves on the membrane lead to complex vibrations.

striking cases energy in the ring was present, still when striking in the ring the energy was even stronger.

The two lower plots in Fig. 7 show the laser interferometry measurements for sinusoidal excitation at 918 Hz inside the ring on the left and outside on the right. Clearly when

driving inside the ring nearly all amplitude are within the ring, while when driving outside nearly all amplitudes are outside the ring, while the ring boundary cloaks the inner ring area.

Clearly the ring is cloaking vibrations in both directions, from within the ring to its outside and vice versa for

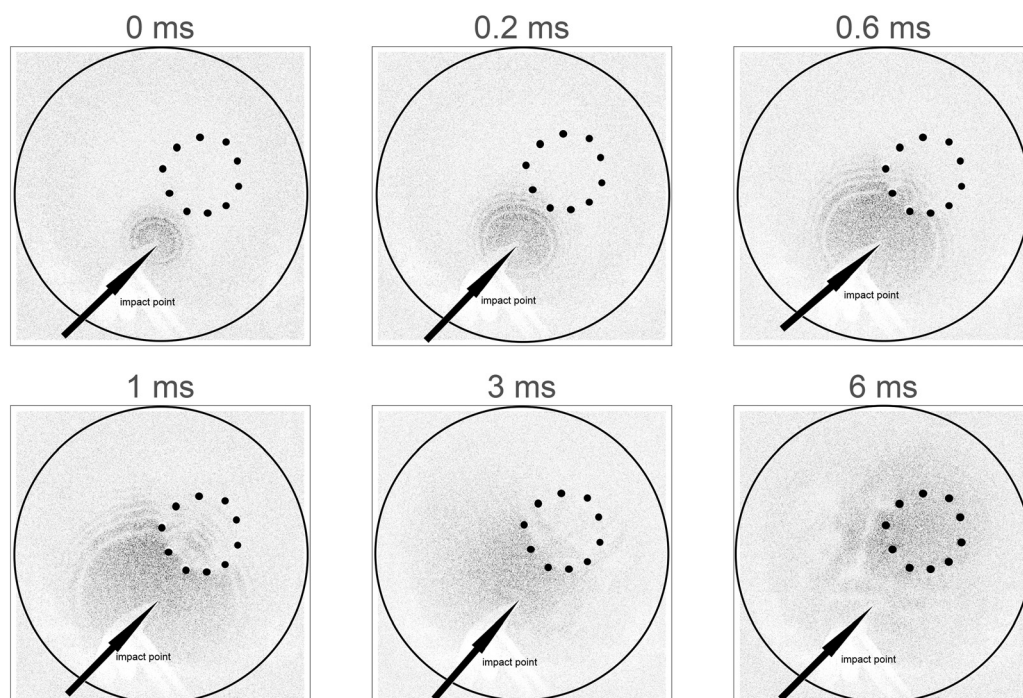


FIG. 6. Laser interferometry measurement of a hammer strike on a membrane with a separated ring area, striking outside the ring. One transition between black and white corresponds to a displacement amplitude of half the laser light wavelength. A circular wavefront leaves the strike position and reaches the ring boundary at 0.2 ms. The boundary leads to a formation of a Huygens wavefront inside the ring from about 0.6 ms. From 1 ms on the vibrations inside the ring are much less than those outside. After about 6 ms there is motion inside the ring, still at small wave vectors and therefore at low frequencies only.

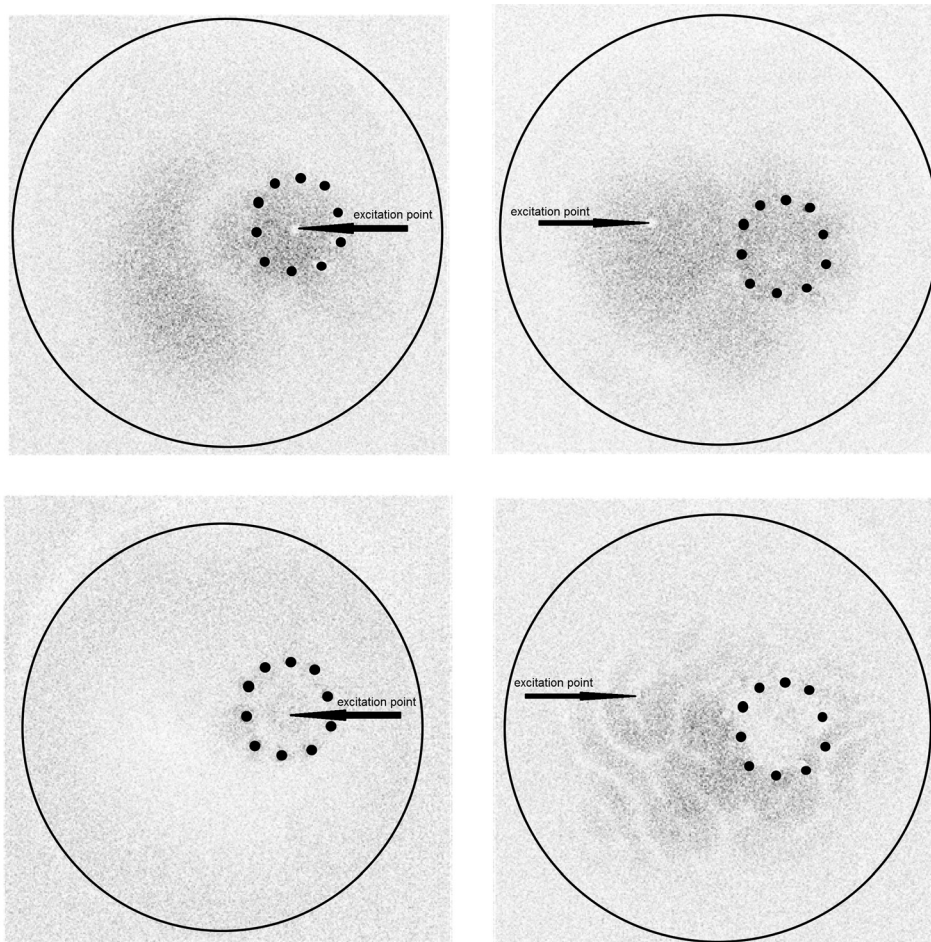


FIG. 7. Snapshots of forced oscillations at 65 Hz (top row) and 918 Hz (bottom row) inside (left column) and outside (right column) the ring. At the low frequency at 65 Hz the vibrations are strong both inside and outside the ring. At the high frequency of 918 Hz the driving of the membrane inside the ring only leads to a vibration inside, while driving the membrane outside the ring the movement is only outside the ring and very low amplitudes are present in the ring. Therefore, the ring at this frequency of 918 Hz acts as a cloaking of waves in both directions. Comparing with Fig. 4 allows the conclusion that above about 400 Hz the ring acts as a cloaking element.

frequencies above about 400 Hz. For frequencies below 400 Hz it is cloaking in a way that vibrations from outside do not enter the ring. Still, when driving the ring some vibrations escape the ring and form modes outside. But also in this case the ring is not taking part in the vibrations considerably. For very low frequencies the cloaking becomes ineffective which is caused by large anti-nodal areas on the membrane.

B. Example sounds

The drum sounds considerably different when struck inside or outside the ring. Within the ring a sound is produced not known from regular drums, while when struck outside a normal drum sound appears. To display this aural finding the drum was struck at three positions only recording the sound with a single microphone 50 cm in front of the membrane opposite to the drum center in an anechoic chamber. With a wooden hammer the drum was struck right at the center of the ring, at the ring boundary between the magnets at a place most close to the membrane center, and outside the ring opposite to it, still with the same distance to the membrane boundary as the ring center, which is 13.5 cm.

Additionally, to test the influence of different ring diameters, next to the 10 cm diameter used for the measurements above, two additional rings were built, one with 8 cm and one with 12 cm in diameter. All had the same center point of the ring as the 10 cm ring, i.e., 13.5 cm in radial distance to the membrane boundary.

The sounds produced here are exemplary. A vast variety of sounds can be produced utilizing hammers of different geometries, elasticities, and hardnesses. The test strikes were performed with musical accuracy providing best possible uniformity in speed, strength, and impact position. As the resulting sounds were so considerably different and this difference maintained when using different striking strength, the overall sound difference between the striking points is clearly documented by this method.

Figure 8 shows the nine strikes, three diameters combined with the three striking positions. Each spectrum was calculated with a Fourier transform of the first 50 ms of the sound. As the drum is a percussion instrument the sound character is mainly heard during this initial sound phase. So, the results presented here only refer to the initial transient.

In the top plot the spectra for the strikes inside the drum are displayed. They show a band gap starting from about 300–400 Hz up to about 700–800 Hz. The low frequencies are still strong, which also holds for the higher ones.

Contrarily, the strikes outside the membrane displayed at the bottom of Fig. 8 show no such band gap but rather a regular spectrum exponentially decaying with frequency. The strike at the ring boundary displayed in the middle plot shows a mixture of both plots, again with an unusual flat spectrum, not considerably decaying towards the higher frequencies.

Both the spectra of the strike inside the ring and that at its boundary cannot be produced by a regular drum. But as

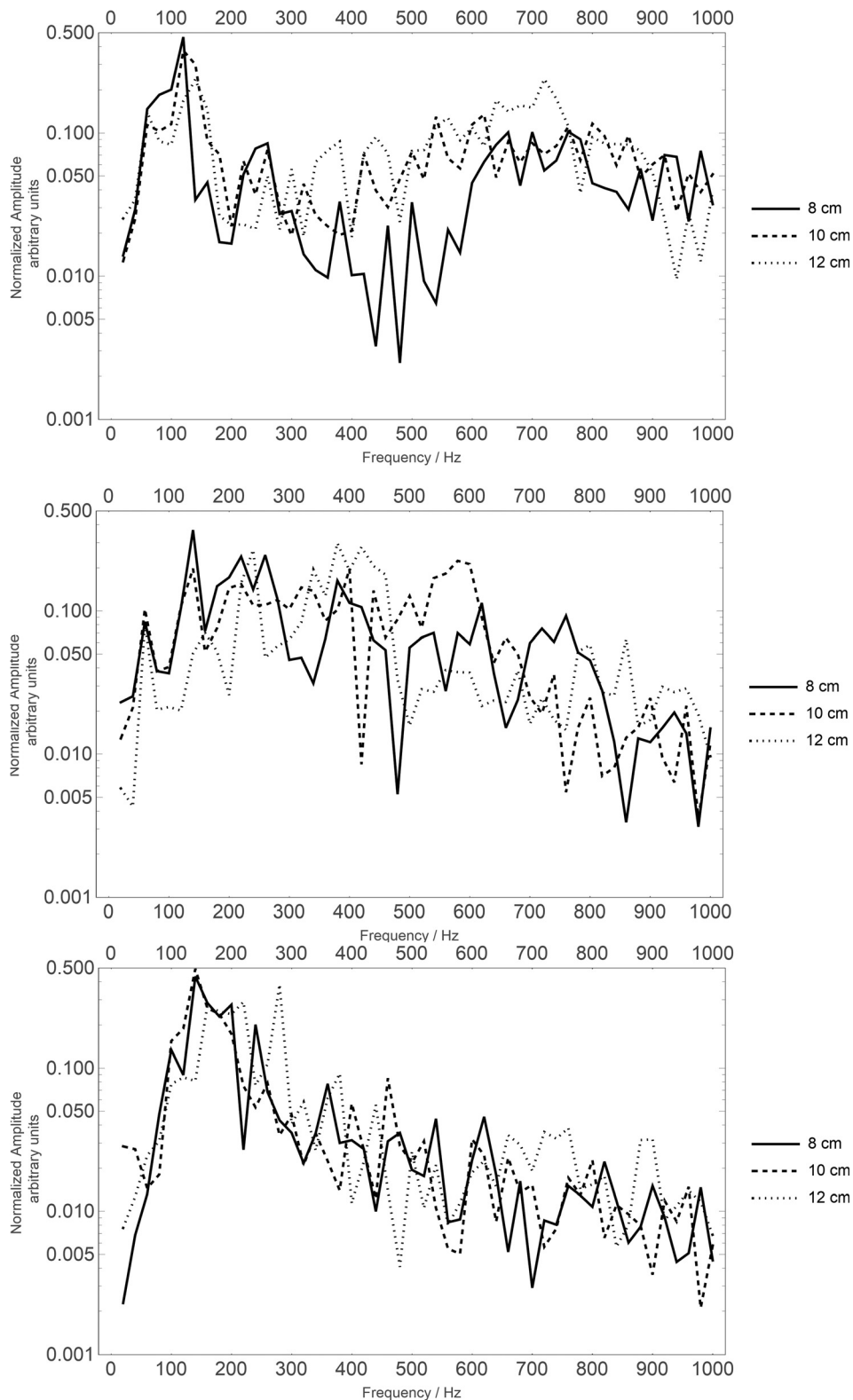


FIG. 8. Spectra of example strikes on the modified membrane for three ring diameters, 8, 10, and 12 cm, as Fourier analysis of the first 50 ms of sound; top: strike position at the ring center; middle: strike position at the ring boundary; bottom: strike position outside the ring. The strikes inside the ring show a band gap between 300/400 and 700/800 Hz, the strikes outside the ring show regular decaying overtone spectra, the strike at the ring boundary are in the middle between inside and outside strikes.

the drum can still be played outside the ring with regular spectral shape, it can still produce normal drum sounds. So, adding the ring increases the articulatory possibilities of the drum considerably.

C. Theoretical considerations

From this parametric study we can make estimations on the frequency onset and offset of the band gap.

1. Band gap upper cut-off frequency

From the lowest frequency of the membrane without the ring of $f_0 = 78$ Hz one finds a wave speed $c = f_0 J^0 / (2\pi r) = 44.8$ m/s, where $J^0 = 2.405$ is the first zero crossing of the Bessel function as radial solution of the circular membrane wave equation with boundary conditions of zero displacement and drum radius $r = 0.2$ m. The wavelength λ fitting between two adjacent magnets of the ring is

$$\lambda_i = 2\pi r_i / m_n - m_d \quad (1)$$

with index $i = 1, 2, 3$ for the three rings with radii $r_1 = 0.04$ m, $r_2 = 0.05$ m and $r_3 = 0.06$ m. Here $m_d = 0.005$ m is the magnet diameter subtracted from a $1/m_n$ of the ring circumference, with $m_n = 10$ the amount of magnets. The frequencies of these wavelength then are $f_i = c/\lambda_i$, and therefore $f_1 = 2027$ Hz, $f_2 = 1545$ Hz, and $f_3 = 1247$ Hz.

These frequencies are about twice the upper cut-off frequency of the band gap at about 700–800 Hz. Therefore, the cloaking behaviour disappears when the gap between the magnets is half the wavelength of the respective frequency. In Fig. 5 (top plot) the tendency of smaller ring diameters to have a larger band gap can clearly be seen. The 8 cm ring has a much larger band gap up to about 800 Hz, the 10 cm ring has a spectral peak at about 550 Hz and the 12 cm ring has also a peak at about 550 Hz but is much less damped before this frequency range. Indeed, the band gap has a small amplitude slope in and out and is not a straight cut at the cutoff-frequencies (has a low Q when taken as a filter). This is expected as the calculated frequencies assume perfectly rigid magnets with infinite mass which is not the case. Clearly the higher cut-off frequency is determined by the ring size.

As found with the microphone array and the laser interferometry data, the magnets prevent the waves within the band gap to leave or to enter the ring. The corresponding wavelengths are much longer than the distances between the magnets. Therefore, the magnet geometry is sub-wavelength and therefore the effect is not a simple scattering but a cloaking of waves. When struck in the ring these band gap frequencies stay within the ring and therefore have a much smaller radiation area compared to waves traveling over the whole membrane, the lower and higher frequencies. This leads to lowered amplitudes of the band gap frequencies in the radiated sound.

2. Band gap lower cut-off frequency

Estimating the frequencies within the rings by taking the magnets as boundary conditions of zero displacement we find $f_1^0 = 390$ Hz, $f_2^0 = 312$ Hz, and $f_3^0 = 260$ Hz. This is not perfectly true, of course, and the movement present at the magnets might be taken as an enlargement of the radii to come closer to the real values. Still, the values are around the frequency range where the band gap start. This confirms the finding of the microphone array data and the laser data. Frequencies below the eigenresonance of the ring appear over the whole membrane and are therefore not damped in the spectrum as those above the fundamental frequencies of the ring.

The ring diameter does not change this overall behaviour, still the 8 cm diameter has the strongest band gap, while the 10 and 12 cm rings perform similar (Fig. 8 top). This also holds for the strike at the ring boundary. Aurally, indeed the ring with the smallest diameter of 8 cm showed this band gap effect most clearly.

IV. CONCLUSIONS

The cloaking of the ring is frequency-dependent because the ring is not in a free-field but on a membrane which again

has boundaries leading to eigenmodes of the whole system. For high frequencies above 300–400 Hz, the eigenmode shapes outside the ring are complex enough that the membrane acts very much like a free field and therefore the regular cloaking behaviour appears. For lower frequencies below 300–400 Hz, cloaking still works in one direction. Here, waves from outside the ring do not considerably enter the ring; still, waves from within the ring can leave to the outside area. For very low frequencies, the cloaking then nearly vanishes. Above about 700–800 Hz, the waves again travel freely over the ring boundary as the wavelengths are smaller than the distances between the magnets.

The transient laser interferometry measurements also show that when striking the drum in the ring, at the very beginning of the sound, some energy leaves the ring. These vibrations trigger the modes between about 100 and 400 Hz outside the ring and those above the upper cut-off frequency of the band gap. This offers another musical option to decide which frequency range to drive when striking in or outside the ring.

It also appears that when striking at the rim of the ring, a mixture of the two extremes, striking outside the ring or at the very center of it can be achieved. This holds for both the frequency range up to about 400 Hz and that above this range.

Furthermore, the cloaking of the ring leads to a different radiation behaviour of the drum compared to when struck outside the ring. When at higher frequencies only the ring area vibrates, it acts like a monopole and radiates sound from a clearly defined point. When striking outside the ring, complex modes appear with a completely different radiation behaviour. Therefore, depending on the driving point, the same frequency might have two completely different radiation patterns. As a monopole radiation is perceived as a loudspeaker-like source, while a complex radiation pattern is perceived as a musical instrument played live, a musician has a new kind of articulation with such a manipulated drum.

The drum shows a much higher amount of timbre variability compared to a regular drum. With regular drums, the drummer can only vary the sound by striking at different positions, where striking in the middle leads to a sound dominated by low frequencies and striking more to the edge increases the amount of energy at higher frequencies, making the sound more bright. Although when striking outside the ring with the presented manipulated drum these articulations are still possible, additionally the drummer is able to produce completely new sounds when striking the membrane at different positions within the ring.

When striking at the very center, even very strongly, the sound has only energy in the low frequencies, with a band gap from 300–400 to 700–800 Hz. Higher frequencies appear only in the initial transient as they decay naturally very fast. The amplitude attenuation in the band gap increases with smaller ring diameters. This sound is not known from a regular drum struck in its middle as, due to the transient behaviour of such a strike and the band gap discussed above at the very beginning of the tone, higher partials are present more than with a regular drum struck at the drum center.

Therefore, such a sound is not possible to produce for drummers with regular drums.

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